

# Static and Dynamic Structure of $\text{Au}_2\text{Cl}_6$ , $\text{AuAlCl}_6$ and $\text{AuFeCl}_6$ Clusters

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Z. Naturforsch. **55 a**, 495–498 (2000); received February 12, 2000

Fourfold coordination of trivalent metal ions by chlorines in molecular dimers changes from tetrahedral in  $\text{Al}_2\text{Cl}_6$  and  $\text{Fe}_2\text{Cl}_6$  to planar in  $\text{Au}_2\text{Cl}_6$ . Within an ionic model we interpret this transition in the stable molecular shape as due to the quadrupolar polarizability of the gold(III) ion. We also demonstrate within the same model that a mixed tetrahedral-planar coordination is stable in  $\text{AuAlCl}_6$  and  $\text{AuFeCl}_6$  clusters. Quantitative comparisons are presented for the calculated molecular structures and vibrational frequencies against the available experimental data from crystalline diffraction and from Raman spectra of the crystal and of vapours.

**Key words:** Ionic Clusters; Molecular Vapours; Molecular Crystals.

## 1. Introduction

The crystal structure of gold(III) chloride as determined by Clark *et al.* [1] can be viewed as formed from lattice cells containing pairs of planar  $\text{Au}_2\text{Cl}_6$  molecules and arranged in a monoclinic ordering. Inside one of these molecules, each gold ion is coordinated by two bridging and two terminal chlorines lying at the corners of a slightly deformed square. Nalbandian and Papatheodorou [2] measured the Raman spectra of this solid compound and performed a normal mode analysis of the measured spectrum on the basis of the known crystal structure, obtaining a complete force field. They further showed that this force field yields agreement with some measured Raman modes both for the  $\text{Au}_2\text{Cl}_6$  molecule in the vapour and for the  $\text{AuAlCl}_6$  vapour complex, the latter being formed as a minority species in  $\text{Al}_2\text{Cl}_6$  vapours over solid gold(III) chloride [3]. In their analysis they assumed for the  $\text{AuAlCl}_6$  molecule a structure which is intermediate between the tetrahedral coordination existing in the  $\text{Al}_2\text{Cl}_6$  molecule [4] and the square-type coordination in  $\text{Au}_2\text{Cl}_6$ .

While a tetrahedral-type coordination by halogens is quite common for trivalent-metal ions in low-density (liquid and vapour) states [5], the planar structure of  $\text{Au}_2\text{Cl}_6$  is very striking and apparently as yet not accounted for in a theoretical model. If for simplicity we contrast these two types of coordination in the  $\text{AlCl}_4$  and  $\text{AuCl}_4$  molecular-ion monomers, we

may view the  $\text{AuCl}_4$  square as arising from the  $\text{AlCl}_4$  tetrahedron under lowering of three-dimensional rotational symmetry. From this viewpoint there should be little doubt that the main driving force for such symmetry breaking is the high quadrupolar polarizability of the gold(III) ion.

In the present work we evaluate the equilibrium structures and the vibrational spectra of the  $\text{Au}_2\text{Cl}_6$ ,  $\text{AuAlCl}_6$ , and  $\text{AuFeCl}_6$  molecules by means of a microscopic ionic model. We start from our earlier studies of  $\text{Al}_2\text{Cl}_6$ -based clusters [6] and of the  $\text{Fe}_2\text{Cl}_6$  and  $\text{AlFeCl}_6$  molecules [7] and augment them by inclusion of the interactions between ionic charges and induced quadrupoles. The model includes as free parameters the ionic radius and the quadrupole polarizability of gold(III). Through a sensible estimation of these parameters, we can assess the equilibrium structures of the three molecules of present interest and obtain a rather good overall account of the available experimental evidence.

## 2. Interionic Force Model

In our earlier studies of trivalent-metal chlorides [6, 7] we constructed an expression for the potential energy  $U(\{\mathbf{r}_{ij}\}, \{\mathbf{p}_i\})$  of an ionic cluster as a function of the interionic bond vectors  $\mathbf{r}_{ij}$  and of the electric dipole moments  $\mathbf{p}_i$ . This was based on a suitable extension of the shell model (also known as the deformation dipole model) for the lattice dynamics of ionic

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Table 1. Interionic force parameters in Au<sub>2</sub>Cl<sub>6</sub>.

	$z_{\text{Au}}$	$z_{\text{Cl}}$	$R_{\text{Au}}$ (Å)	$\rho_{\text{Au}}$ (Å)	$R_{\text{Cl}}$ (Å)	$\rho_{\text{Cl}}$ (Å)	$C_{\text{Cl}}$ (eÅ <sup>5/2</sup> )	$\alpha_{\text{Cl}}$ (Å <sup>3</sup> )	$\alpha_s$ (Å <sup>3</sup> /e)	$Q_{\text{Au}}$ (e <sup>2</sup> Å <sup>5</sup> )
Al-like	2.47 <sub>2</sub>	−.82 <sub>4</sub>	1.16	0.054	1.71	0.238	5.5	2.05	0.46	9.5
Fe-like	2.30 <sub>4</sub>	−.76 <sub>8</sub>	1.13	0.049	1.71	0.238	5.5	2.72	0.66	9.5

and semiconductor crystals [8]. A basic quantum mechanical justification for this approach to molecular structure has been given for alkali halides by means of exchange perturbation theory [9, 10]. For the detailed expressions entering  $U(\{\mathbf{r}_{ij}\}, \{\mathbf{p}_i\})$  we refer to our earlier work [6].

In dealing with gold(III)-based chlorides we extend the exchange perturbation approach to include the induction of a quadrupolar moment on gold(III) by the ionic charges in the molecule. The relevant quantity is, of course, the electric field gradient  $E_{\alpha\beta}$ . Considering first an AuCl<sub>4</sub> molecular ion, we write

$$E_{\alpha\beta} = \sum_{i=1}^4 \left[ -3 \frac{R_{i\alpha} R_{i\beta}}{R_i^5} + \frac{1}{R_i^3} \delta_{\alpha\beta} \right], \quad (1)$$

where  $\mathbf{R}_i$  is the vector joining Au to the  $i$ -th Cl and a Greek suffix denotes a Cartesian component. The interaction energy with the quadrupolar moment  $Q_{\alpha\beta}$  on Au thus is

$$U_Q = \sum_{\alpha,\beta} Q_{\alpha\beta} E_{\alpha\beta}. \quad (2)$$

Since the quadrupole moment  $Q_{\alpha\beta}$  is in fact induced by the electric field gradient, we have for a planar-molecule (lying in the  $(x, y)$  plane, say) the result

$$U_Q = -Q \sum_{i=1}^4 \frac{R_{ix}^4 + R_{iy}^4}{R_i^{10}}, \quad (3)$$

where  $Q$  is a constant measuring the quadrupolar polarizability of gold(III). We have obtained a first estimate of this quantity by starting from a (stable) tetrahedral shape for AuCl<sub>4</sub> at  $Q = 0$  and by increasing  $Q$  until the stable shape has become a square.

For a full assessment of the model parameters describing the gold-based chloride clusters, we have assumed transferability of a number of parameters between different systems as in our earlier studies and adjusted the quadrupolar parameter  $Q_{\text{Au}}$  and the ionic radius  $R_{\text{Au}}$  to the known structure of the Au<sub>2</sub>Cl<sub>6</sub>

molecule in the gold trichloride crystal [1]. The transferred parameters are (i) the effective valences  $z_{\text{Cl}}$  and  $z_{\text{Au}} = -3z_{\text{Cl}}$ , (ii) the electric dipole polarizability  $\alpha_{\text{Cl}}$ , the short-range polarizability  $\alpha_s$  and the van der Waals coefficient  $C_{\text{Cl}}$  for the chlorines, (iii) the ionic radius  $R_{\text{Cl}}$  and the stiffness parameter  $\rho_{\text{Cl}}$  describing the contribution of the chlorines in the Busing form [11] of the Au-Cl overlap repulsions, and (iv) the ratio  $R_{\text{Au}}/\rho_{\text{Au}}$  of the analogous quantities for gold(III). We have tested the reliability of this transfer by evaluating two alternative choices of these parameters, *i. e.* their values obtained in our earlier studies of Al<sub>2</sub>Cl<sub>6</sub> [6] and of Fe<sub>2</sub>Cl<sub>6</sub> [7]. In the following we refer to these two choices as “Al-like” and “Fe-like”.

Table 1 shows the two alternative sets of model parameters that we have used in the calculations reported in the sequel. Of course, in dealing with AuAlCl<sub>6</sub> and with AuFeCl<sub>6</sub> we have used the Al-like and Fe-like sets of parameters, respectively.

### 3. Equilibrium Structures

The calculated equilibrium shape of the Au<sub>2</sub>Cl<sub>6</sub> molecule is shown in Figure 1. Table 2 reports the values of its structural parameters, in comparison with the data on Au<sub>2</sub>Cl<sub>6</sub> molecules in gold trichloride crystals from the experiments of Clark *et al.* [1]. The symbols Cl<sup>T</sup> and Cl<sup>B</sup> denote a terminal and a bonding chlorine, respectively.

It is evident from Table 2 that there is substantial agreement between the results obtained with the

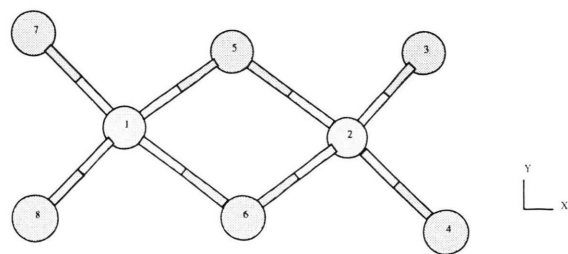


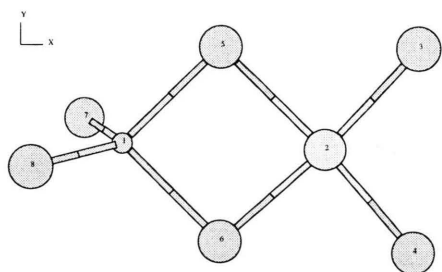
Fig. 1. A ball-and-stick model of the structure of the Au<sub>2</sub>Cl<sub>6</sub> molecule, showing the two gold(III) ions in a distorted square coordination by chlorines.

Table 2. Equilibrium structure of  $\text{Au}_2\text{Cl}_6$  (bond lengths in Å, bond angles in degrees).

	Au-Cl <sup>T</sup>	Au-Cl <sup>B</sup>	Au-Au	$\angle \text{Cl}^{\text{T}}\text{-Au-Cl}^{\text{T}}$	$\angle \text{Cl}^{\text{B}}\text{-Au-Cl}^{\text{B}}$
Al-like	2.21	2.36	3.61	99.4	80.4
Fe-like	2.24	2.37	3.53	98.5	83.7
Crystal [1]	2.24	2.33	3.41	90.0	86.0

Table 3. Equilibrium structure of  $\text{AuAlCl}_6$  and  $\text{AuFeCl}_6$  (first and third row), in comparison with those of  $\text{M}_2\text{Cl}_6$  and  $\text{Au}_2\text{Cl}_6$  for  $\text{M} = \text{Al}$  (second row) and  $\text{M} = \text{Fe}$  (fourth row).

M-Cl <sup>T</sup>	M-Cl <sup>B</sup>	Au-Cl <sup>T</sup>	Au-Cl <sup>B</sup>	$\angle \text{Cl}^{\text{T}}\text{-M-Cl}^{\text{T}}$	$\angle \text{Cl}^{\text{B}}\text{-M-Cl}^{\text{B}}$	$\angle \text{Cl}^{\text{T}}\text{-Au-Cl}^{\text{T}}$	$\angle \text{Cl}^{\text{B}}\text{-Au-Cl}^{\text{B}}$
2.07	2.25	2.21	2.37	121	88	99	82
2.06	2.28	2.21	2.36	121	90	99	80
2.16	2.31	2.24	2.38	120	90	98	87
2.15	2.33	2.24	2.37	120	94	98	84

Fig. 2. A ball-and-stick model of the structure of the  $\text{AuAlCl}_6$  and  $\text{AuFeCl}_6$  molecules, showing the gold(III) ion in a distorted square coordination and the other trivalent metal ion in a distorted tetrahedral coordination.

two alternative sets of model parameters, both sets of results being in very reasonable agreement with the crystal diffraction data.

Figure 2 shows the calculated equilibrium shape of the  $\text{AuAlCl}_6$  molecule. As proposed by Nalbandian and Papatheodorou [2], it can be viewed as obtained from matching the tetrahedral structure of  $\text{AlCl}_4$  with a square structure for  $\text{AuCl}_4$  through bridging by a pair of chlorines. The quantitative extent to which this is true is shown in Table 3 by reporting the structural parameters of  $\text{AuAlCl}_6$  in comparison with those of  $\text{Al}_2\text{Cl}_6$  [6] and of  $\text{Au}_2\text{Cl}_6$  (see Table 2). Evidently, it is an excellent approximation to take the values of bond lengths and bond angles in the mixed molecule from the parent dimers. We obtain qualitatively similar results for the  $\text{AuFeCl}_6$  molecule (see Table 3).

In concluding this section we remark that from our calculations we find that the induced-quadrupole

Table 4. Frequencies of vibrational modes for  $\text{Au}_2\text{Cl}_6$  (in  $\text{cm}^{-1}$ ).

		$\text{Au}_2\text{Cl}_6$ -calc.		$\text{Au}_2\text{Cl}_6$ -meas. [2]	
		Al-like	Fe-like	Crystal	Vapour
$A_g$	$\nu_1$	376	360	378	386
	$\nu_2$	327	325	327	324
	$\nu_3$	166	158	166	157
	$\nu_4$	103	103	97	96
$A_u$	$\nu_5$	89	86	—	—
$B_{1g}$	$\nu_6$	364	350	365	—
	$\nu_7$	237	238	288	—
$B_{1u}$	$\nu_8$	135	129	122	—
	$\nu_9$	161	153	135	—
$B_{2g}$	$\nu_{10}$	73	69	—	—
	$\nu_{11}$	115	109	104	—
$B_{2u}$	$\nu_{12}$	382	365	383	—
	$\nu_{13}$	283	280	313	—
$B_{3g}$	$\nu_{14}$	100	95	80	—
	$\nu_{15}$	112	107	—	—
$B_{3u}$	$\nu_{16}$	365	350	373	—
	$\nu_{17}$	278	279	309	—
	$\nu_{18}$	165	157	143	—

contribution to the binding energy of these molecules is quite appreciable, of the order of 3.6 - 3.9 eV per gold ion. In spite of this we find that both mixed molecules are somewhat more strongly bound than the  $\text{Au}_2\text{Cl}_6$  one, by about 2 eV in the case of  $\text{AuAlCl}_6$  and by almost 1 eV in the case of  $\text{AuFeCl}_6$ .

#### 4. Vibrational Frequencies

The calculated vibrational frequencies of the molecules whose structure we have evaluated in Sect. 3 are reported in Tables 4 and 5. Table 4 compares our results for the  $\text{Au}_2\text{Cl}_6$  molecule with the Raman scattering data of Nalbandian and Papatheodorou [2] on both the gold trichloride crystal and the gaseous molecule. In Table 5 we give our results for the mixed  $\text{AuFeCl}_6$  and  $\text{AuAlCl}_6$  molecules, together with the values measured by the same authors for the latter molecule. We do not consider fits of the experimental data by the valence force field method.

The agreement between calculated and measured spectra in Tables 4 and 5 can be considered as very reasonable, considering that the calculations have been carried out within a microscopic model of the full molecular potential energy and that none of these data has been fitted in the adjustment of the model parameters. The agreement is quite good for the bond-stretching modes at high frequency, but appears to be somewhat less satisfactory as one moves into the region of bond-bending modes. Again, there is sub-

stantial agreement between the results reported for  $\text{Au}_2\text{Cl}_6$  in Table 4 as obtained from our two alternative sets of model parameters.

## 5. Concluding Remarks

We have in this work described a microscopic model of ionic interactions in gold-based trichlorides, including contributions to the potential energy from induced quadrupoles on the gold(III) ion. Through these contributions we have been able to account for the planar structure of the  $\text{Au}_2\text{Cl}_6$  molecule and to demonstrate the coexistence of distorted tetrahedral and square coordinations in the  $\text{AuAlCl}_6$  and  $\text{AuFeCl}_6$  molecules.

The reasonably accurate description of structural data and vibrational frequencies that we have achieved with the help of a minimal number of free parameters validates the model and suggests that it should find useful applications in further studies of condensed states of these materials.

## Acknowledgements

One of us (ZA) acknowledges support received from the Turkish Scientific and Technological Re-

Table 5. Frequencies of vibrational modes for  $\text{AuFeCl}_6$  and  $\text{AuAlCl}_6$  (in  $\text{cm}^{-1}$ ).

		$\text{AuFeCl}_6$ - calc.	$\text{AuAlCl}_6$ -calc.	$\text{AuAlCl}_6$ - meas. [2]
$A_1$	$\nu_1$	411	507	495
	$\nu_2$	350	380	386
	$\nu_3$	325	358	(330)
	$\nu_4$	270	284	300
	$\nu_5$	161	191	183
	$\nu_6$	122	140	156
	$\nu_7$	90	97	(98)
$A_2$	$\nu_8$	107	113	—
	$\nu_9$	68	73	—
$B_1$	$\nu_{10}$	460	616	—
	$\nu_{11}$	151	170	—
	$\nu_{12}$	112	133	—
	$\nu_{13}$	56	60	—
$B_2$	$\nu_{14}$	363	382	—
	$\nu_{15}$	341	360	—
	$\nu_{16}$	219	220	—
	$\nu_{17}$	151	162	—
	$\nu_{18}$	87	94	—

search Council (Tubitak) and from the Research Fund of the University of Istanbul under Project Number Ö-681/121099. She also wishes to thank the Scuola Normale Superiore di Pisa for their hospitality during the final stages of this work.

- [1] E. S. Clark, D. H. Templeton, and C. H. MacGillavry, *Acta Crystallogr.* **11**, 284 (1958).
- [2] L. Nalbandian and G. N. Papatheodorou, *Vibrat. Spectrosc.* **4**, 25 (1992).
- [3] L. Nalbandian, S. Boghosian, and G. N. Papatheodorou, *Inorg.Chem.* **1992**, 1769.
- [4] R. L. Harris, R. E. Wood, and H. L. Ritter, *J. Amer. Chem. Soc.* **73**, 3150 (1951).
- [5] For a recent review see Z. Akdeniz, D. L. Price, M.-L. Saboungi, and M. P. Tosi, *Plasmas and Ions* **1**, 3 (1998).
- [6] Z. Akdeniz and M. P. Tosi, *Z. Naturforsch.* **54a**, 180 (1999).
- [7] Z. Akdeniz and M. P. Tosi, *Z. Naturforsch.* **54a**, 477 (1999).
- [8] See e. g. R. A. Cochran, *Crit. Rev. Solid State Sci.* **2**, 1 (1971); J. R. Hardy and A. M. Karo, *The Lattice Dynamics and Statics of Alkali Halide Crystals*; Plenum Press, New York 1979.
- [9] M. P. Tosi and M. Doyama, *Phys. Rev.* **160**, 716 (1967).
- [10] P. Brumer and M. Karplus, *J. Chem. Phys.* **58**, 3903 (1973).
- [11] W. R. Busing, *Trans. Amer. Crystallogr. Assoc.* **6**, 57 (1970).